



## **The Effect of GeoGebra in Three-Dimensional Geometry Learning on Students' Mathematical Communication Ability**

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The purpose of this research is to analyze the effect of GeoGebra in three-dimensional geometry learning on students' mathematical communication ability as a whole and based on students' prior mathematical abilities. This quasi-experimental research with randomized posttest only design included 84 XII grade students in high school in Central Jakarta, Indonesia. Before the research, students were grouped based on their prior mathematical abilities including high, medium and low groups. The research data were the results of mathematical communication skills tests consisting of 7 questions which were then analyzed by Mann-Whitney test. The results reveal that overall and for students with high and medium mathematical prior abilities, there were significant differences in mathematical communication skills between students who received GeoGebra assisted Geometry learning and students who obtained conventional mathematics learning, while for students with low prior mathematical ability, there is no significant difference.

**Keywords:** GeoGebra, three-dimensional geometry, mathematical communication ability, prior mathematical ability, quasi-experimental

### **INTRODUCTION**

Mathematical communication ability is one of the important mathematical thinking abilities to improve. The National Council of Teachers of Mathematics (NCTM) and the Indonesian Ministry of Education and Culture set mathematical communication skills as one of the standard abilities students must possess in learning mathematics (NCTM, 2000) (Ministry of Education and Culture, 2016). Mathematical communication ability

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is a way to share mathematical ideas and clarify understanding of a mathematical idea. (NCTM, 2000).

Mathematical communication ability helps students building conceptual understanding of a concept and providing opportunities for students to clarify their understanding and consolidate mathematical ideas (Hirschfeld-Coton, 2008). Mathematical communication has an important role in learning mathematics because through mathematical communication students can express, explain, describe, and listen to an understanding of mathematics (Paridjo, 2017). Communication ability is needed to understand mathematical ideas appropriately. Weak communication ability will weaken other mathematical abilities. Students who have high mathematical communication ability can make diverse representations and is easier to find alternative solutions to problem solving (Qohar, 2011).

One material that requires mathematical communication skills is geometry. Geometry is one of the essential materials in the Indonesian curriculum and taught to students from elementary school to the level of lectures (Jelatu et.al, 2018). Therefore, it is important to improve students' mathematical communication ability, especially in the field of geometry.

On the other hand, there is a fact that the mathematical communication ability of Indonesian students is still low. Mathematical communication ability included in levels 5 and 6 in the PISA assessment (PISA, 2015). The 2015 PISA results show that scores of Indonesian students for level 5 and 6 only range from 0 - 0.6% (PISA, 2015). More specifically in learning geometry in the classroom, there are many difficulties encountered by teachers and students because geometric learning involves more abstract concepts than concrete concepts (Tutkun&Ozturk, 2013). Geometry learning which is presented textually by using pencils and paper and involves concepts that are not related to students' contexts causes students difficulties in understanding the various geometric concepts presented (Jelatu, 2017).

The low mathematical communication ability of students, especially in geometry material, is closely related to the learning process in class. The integration of technology in education, especially in mathematics learning, becomes an important matter and is becoming a trend (Azizul& Din, 2016). One software that can be used in geometry learning is GeoGebra. Geometry learning using GeoGebra can help students to see abstract concepts, make connections, and discover mathematical concepts (Antohe, 2009). This study will analyze the effect of GeoGebra in learning three-dimensional geometry to ward students' mathematical communication ability as a whole and based on prior mathematical abilities.

### **GeoGebra in Three-Dimensional Geometry Learning**

GeoGebra is software that is freely available for teaching and learning mathematics with features suitable for topics such as geometry and algebra (Azizul& Din, 2016). GeoGebra is a dynamic software that addresses the concepts of Geometry, Algebra, and

Calculus (Hohenwarter et.al, 2010). GeoGebra can be used to strengthen students' understanding of concepts that have been used and as a means to express or construct new concepts (Hohenwarter et.al, 2008). GeoGebra software is an interactive media that allows students to explore various mathematical concepts. The use of GeoGebra in learning can help teachers improve student understanding of mathematical concepts and procedures (Hutkemri & Zakaria, 2012) (Zulnaldi, H., & Zamri, 2017). GeoGebra facilitates interactive assessment to help people involved in the learning process (Murni et.al, 2017).

The following is one example of using GeoGebra in learning three-dimensional geometry to determine the distance between point and fields:

"Suppose ABCDEFGH is a cube with  $AB = 5$ . We will find a distance point F to the ACH field."

The steps to determine the distance of point F to ACH fields using GeoGebra are as follows:

1. Create an ABCDEFGH cube on Geogebra.
2. To create an ACH field, select "Polygon" then click points A, C, H, A respectively.
3. Draw a line through F and perpendicular to the ACH field by clicking "Perpendicular Line", click "poly1" then also click "F".
4. To mark the intersection, select "Intersect" then click line "b" and click "poly1" so that the "I" point is obtained.
5. To calculate the distance, just click "Distance or length" then click "I" and "F", then JF distance will appear.

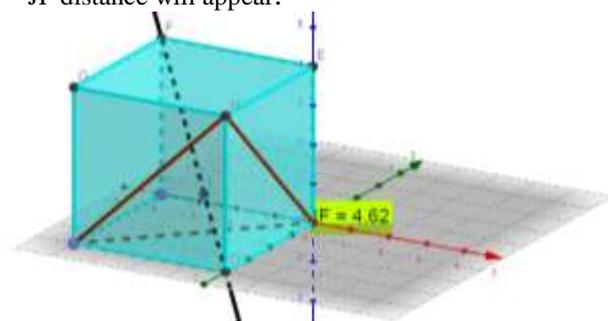


Figure 1  
Mathematical Communication Ability

Communication ability includes activities such as active listening, asking questions and answering questions, giving explanations, and effective debate techniques (NCTM, 2000). Communication is the process of expressing mathematical ideas and understanding verbally, visually, and in writing, using numbers, symbols, images,

graphics, diagrams, and words. Students communicate for various purposes and different audiences, such as teachers, colleagues, groups of students, or the whole class. Communication is the delivery of meaning through various forms of oral, written, and visual, for example giving explanations of reasoning or justification of results verbally or in writing and communicating mathematical ideas and solutions in writing, using numbers and algebraic symbols, and visually, using images, diagrams, charts, tables, graphs and concrete objects. Through communication, students can reflect on and clarify their ideas, their understanding of the relationship of mathematics, and their mathematical arguments (Ministry of Education Ontario, 2005). Communication through mathematical ideas can be utilized in various perspectives, the way students think can be honed, understand growth can be measured; student thinking can be consolidated and organized; mathematical knowledge and development of student problems can be improved; and mathematical communication can be done (Hidayati, 2016). Mathematical communication ability can be built by observing explaining concepts, differentiating a mathematical concept, proposing theories, describing problems by manipulating images or graphics and explaining the results of one's own thinking. (Whitin, 2002). Communication ability is one of the factors that contribute to determining student success in solving problems (Stacey, 2005). According to Zulnaidi, communication is a process that includes interaction and perception. Communication is the exchange of specific information where there is a process of sending verbal messages such as words and nonverbal such as symbols, gestures, etc. Communication always has certain situational characters determined by the relationship between participants (Anatolievna, 2017). Communication is an important part of mathematics and mathematics education. Mathematical learning will be more developed when interactions between students and between teachers and students are established on the basis of good communication skills (Wilkins & Kosko, 2006) Lopatto divides communication skills into 3 types including skills on oral communication, skill at written communication, and skill at visual communication (Lopatto, 2003).

In this study three indicators of mathematical communication ability are used, namely written text, drawing, mathematical expression (Ansari, 2003). The following are presented sub-indicators of each aspect:

Table 1  
Indicators of Mathematical Communication Ability

The Aspect of Mathematical Communication Ability	Indicators of Mathematical Communication Ability
Written Text	Give answers using their own language, make models using or writing using writing and algebra, explain and make questions about mathematics that have been studied, discussed, and written about mathematics, compiling arguments and generalizations.
Drawing	Reflecting real objects, images, and diagrams into mathematical ideas and vice versa
Mathematical Expressions	Express mathematical concepts by expressing daily events in mathematical language or symbols.

## METHOD

### Method and Design

This research uses a quantitative approach with a quasi-experimental method. The quasi-experimental method is used because there are other variables in the study that are difficult to control. This study involved the experimental group, which is the group given the treatment of learning using GeoGebra and the control group, which is the group given the conventional learning model treatment. The design of this study is Randomized Control Group Post Test Only. Researcher wants to analyze the mathematical communication skills of students given learning with GeoGebra and students are given conventional learning. Before the study, students in the experimental and control groups were first grouped based on their prior abilities, namely low, medium, or high. The dependent variable of this study is students' mathematical communication ability while the independent variable is learning using GeoGebra. The research design is illustrated in the following table:

Table 2  
Research Design

Class	Treatment	Post Test
E	X	O
K	-	O

Information:

E: Experimental Class

K: Control Class

X: Application of learning with the Concrete-Pictorial-Abstract (C-P-A) learning model with a knowledge classification strategy

O: Post Test Results

### Participant

The population in this study were grade XII students of State High Schools in Central Jakarta, Indonesia in the academic year 2017/2018. Furthermore, the sample from this study was taken from a population of two classes selected by the Cluster Random Sampling technique. Each was randomly selected to be assigned to the experimental class (the class has given learning with GeoGebra) and the control class (the class has given the conventional learning model). The experimental class consisted of 41 students, 8 students in the high MPK category, 25 students in the moderate MPK category and 8 low MPK categories. The control class consisted of 41 students, 8 students in the high MPK category, 26 students in the moderate MPK category and 7 students in the low MPK category. This situation can be shown in the following table:

Table 3  
Number of Students by MPK

		Class	
		Experiment	Control
Prior Mathematical Ability	High	8	8
	Moderate	25	26
	Low	8	7

### Data Collection

The data in this study were obtained from the results of the student's mathematical communication ability test from experiment and control class on the three-dimensional material given after the learning was completed. The mathematical communication ability test instrument used in this study measures three aspects namely written text, drawing, and mathematical expression.

### Data Analysis

The data analysis used in this study is descriptive and inferential statistical analysis. Hypothesis testing is done through t-test and Mann-Whitney test with a significance level of 0.05 where previously normality tests were also carried out with Kolmogorov-Smirnov and homogeneity tests with Levene's test.

### FINDINGS

#### Data on Student Mathematical Communication Ability as a Whole

The results of the descriptive statistics for achieving students' mathematical communication skills as a whole are as follows:

Table 4  
Descriptive Statistics of Students' Mathematical Communication Ability Score as a Whole

Ideal Score	Experiment Class					Control Class				
	N	$x_{min}$	$x_{maks}$	$\bar{x}$	$S_d$	N	$x_{min}$	$x_{maks}$	$\bar{x}$	$S_d$
24	41	14	22	18.46	2.31	41	8	22	15.85	4.02

Students who get GeoGebra learning is better than students who get conventional learning. Tables 5a, 5b and 5c show the results of the normality test. Homogeneity test, T-Test and Mann Whitney test with a significant 0.05.

Table 5a  
Data Normality Test of Student's Mathematical Communication Ability as a Whole

Class	Shapiro-Wilk		Interpretasi
	Df	Sig.	
Experiment	41	0.78	Normal Distribution
Control	41	0.23	Not Normal Distribution

Table 5a shows that the test score data of students' mathematical communication ability for the experimental class are normally distributed and the control class is not normally distributed.

Table 5b  
Test Data Homogeneity of Students' Mathematical Communication Ability as a Whole

Statistic Levene	Sig.
2.83	0.97

It Table 5b, note that the value of sig. > 0.05 that means hypothesis Ho is accepted and H1 is rejected. This means that the data from the experimental and control class as a whole are homogeneous. Furthermore, to find out whether there were differences between the classes that were significantly different, a non-parametric test was performed with the Mann-Whitney test. With the hypothesis: there is no significant difference in the improvement of communication ability between students given Geogebra assisted geometry learning and students who learn mathematics can be seen from the PMK group. To test the hypothesis, the statistical hypothesis is formulated as follows:

Table 5c  
Test the Difference of Student's Mathematical Communication Ability as a Whole

Asymp. Sig. (2-tailed)	Interpretation
0.04	Ho rejected

Based on Table 5c, the value of Sig. <0.05, so reject Ho. This means that there are significant differences in the improvement of mathematical communication skills

between students who get Geogebra assisted Geometry learning and students who get conventional mathematics learning.

### Student Mathematical Communication Ability Data Based on Prior Mathematical Abilities

The results of descriptive statistics for achieving mathematical communication skills of students based on the KAM category are as follows:

Table 6

Descriptive Statistics Mathematical Communication Ability Based on Prior Mathematical Ability

Prior Mathematical Abilities	Ideal Score	Experiment Class					Control Class				
		N	$x_{min}$	$x_{maks}$	$\bar{x}$	$S_d$	N	$x_{min}$	$x_{maks}$	$\bar{x}$	$S_d$
High	24	9	0.43	0.78	0.61	0.13	8	0.13	0.78	0.59	0.27
Moderate		24	0.00	0.75	0.50	0.17	26	0.00	0.71	0.36	0.14
Low		8	0.27	0.77	0.48	0.17	7	0.12	0.45	0.28	0.12

Students who get GeoGebra learning is better than students who get conventional learning. The results of the achievement of students' mathematical communication ability based on high prior mathematical ability, moderate prior mathematical ability, and low prior mathematical ability must meet the difference test requirements between students who receive learning with GeoGebra and students who receive regular learning. Tables 7a, 7b, and 7c show the results of the normality test. Homogeneity test, and Mann Whitney test with a significant 0.05.

Table 7a

Data Normality Test of Student Mathematical Communication Ability Based on Prior Mathematical Abilities

Category		Class	N	Sig. (2-tailed)	Ho	Interpretation
PRIOR MATHEMATICAL ABILITY	High	Experiment	9	0.42	Accepted	Normal
		Control	8	0.63	Accepted	Normal
	Moderate	Experiment	24	0.02	Rejected	Not Normal
		Control	26	0.89	Accepted	Normal
	Low	Experiment	8	0.25	Accepted	Normal
		Control	7	0.95	Accepted	Normal

Table 7a shows that the score data tests students' mathematical communication ability for the experimental and control classes as general except the group with moderate prior ability in the experimental class has a sig value.  $> 0.05$ . Thus,  $H_0$  is accepted and rejected  $H_1$ , meaning that data is normally distributed while the group with moderate prior ability in the experimental class has a sig value.  $< 0.05$  so that it is not normally distributed.

Table 7b

Test the Homogeneity of Students' Mathematical Communication Ability Based on Prior Mathematical Abilities

Prior Mathematical Abilities	Asymp. Sig.	Ho	Interpretation
High	0.04	Rejected	Not Homogeny
Moderate	0.01	Rejected	Not Homogeny
Low	0.06	Rejected	Not Homogeny

In Table 7b it is known that the sig value.  $<0.05$  so the hypothesis  $H_0$  is rejected and  $H_1$  is accepted. This means that there are no homogeneous data from the three groups. Furthermore, to find out whether the differences in the increase in learning outcomes between the experimental class and the control class differed significantly, nonparametric tests were performed with Mann-Whitney test. With the hypothesis: there is no significant difference in the improvement of mathematical communication ability between students who get GeoGebra assisted Geometry learning and students who get conventional mathematics learning in terms of the prior mathematical abilities group. The t-test and Mann-Whitney test results are presented in the table as follows:

Table 7c

Test of Difference in Increased Mathematical Communication Ability Based on Prior Mathematical Abilities

Prior Mathematical Abilities	Asymp. Sig.	Interpretation
High	0.04	Ho rejected
Moderate	0.01	Ho rejected
Low	0.06	Ho rejected

Based on table 7c, it can be concluded that mathematical communication skills based on prior mathematical abilities are obtained, namely:

1. At low prior mathematical abilities levels, there is no significant difference in mathematical communication skills between students who get Geogebra-assisted Geometry learning and students who get conventional mathematics learning in terms of high, medium and low groups
2. At the high and medium level of prior mathematical abilities, there are differences in mathematical communication skills of students who get learning Geogebra assisted geometry is better than students who get conventional mathematics learning in terms of high, medium and low groups.

## DISCUSSION

The findings of this study reveals that students' mathematical communication ability in three-dimensional geometry who given by GeoGebra were higher than students taught with conventional learning. This finding is in line with the results of a study conducted by Jelatu et al. (2018) where it was found that learning with the REACT strategy assisted by GeoGebra supports the achievement of higher understanding of geometric concepts compared to conventional learning. The findings of this study are also in line

with the research of Saha et al (2010) which revealed that the use of GeoGebra improved student performance in learning Geometry coordinates. Research conducted by Akcakin (2018) also revealed that the use of GeoGebra as a dynamic mathematical device can increase student motivation in achieving goals.

The use of GeoGebra in improving mathematical communication skills is closely related to the functions in GeoGebra which can visualize the concept of abstraction geometry so that it can be more interesting and easily understood by students. Revealed that learning with computer media is more effective than conventional learning because it makes students faster in learning a concept compared to conventional learning. (Kusumah, 2010). The research findings of reveal that GeoGebra influences the solution discovery method (Farihah, 2018). GeoGebra supports students discovering new ways of thinking, manipulating, and analyzing mathematical modeling (Jarvis et.al, 2011). GeoGebra supports learning with multiple representations, computations, documentation, and web-friendly features that expand the range of learning (Bu et.al, 2011).

Pedagogical competence is seen as the ability of teachers to manage to learn, the design of teacher learning activities is expected to pay attention to the material, strategy, technology or surrounding culture in helping to realize active, creative, fun and meaningful learning. This software can be used both as a teaching tool to explore and discover mathematical properties and as a tool for the interactive creation of teaching material (Richardson, S., 2009)

The following is presented the differences in answers using GeoGebra with answers in the conventional class in the 3-dimensional mathematical communication problem:

Question:

"Given a cube ABCD. EFGH with a length of AB is 6 cm. Paint it and calculate the distance between Point E and the ADGF field! "

Answers using GeoGebra:

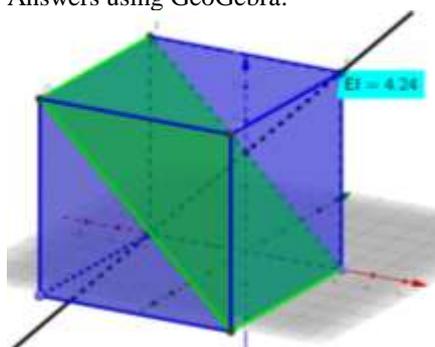


Figure2

The answer in conventional class XII



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